

"Investing in Africa's Future"

FACULTY OF MANAGEMENT AND

# ADMINISTRATION

COURSE TITLE: MMS202 - Quantitative Analysis 1

- **SEMESTER 1:** Final Examination Parallel
- DATE: November 2013
- INSTRUCTOR: Dr. S. Murairwa

TIME: 3 Hours

# INSTRUCTIONS

Answer all questions in Section A and any three (3) questions in Section B

Start each question on a new page in your answer booklet.

The marks allocated to **each** question are shown at the end of the section.

# Show all your workings.

Credit will be given for logical, systematic and neat presentations.

#### SECTION A: ANSWER ALL QUESTIONS

1. A sample of Quantitative analysis I students were asked each to select a toy from a box and the weight of each toy selected was noted. The weights of the toys selected are:

Construct	a steam a	nd leaf fo	r the weig	ht of the to	oys		[4 Marks]
0.58	0.50	0.67	0.94	0.67	0.82	1.00	0.73
0.20	0.85	0.70	0.41	0.66	0.45	0.11	0.83
0.56	0.88	0.37	0.60	0.78	0.69	0.79	0.86
0.57	0.59	0.44	0.36	0.99	0.85	0.44	0.33
0.63	0.73	0.23	0.79	0.74	0.23	0.98	0.83
0.86	0.05	0.46	0.86	0.09	0.72	0.22	0.86
0.11	0.31	0.44	0.95	0.58	0.24	0.23	0.26
0.43	0.15	0.59	0.39	0.82	0.65	0.02	0.15
0.33	0.68	0.51	0.61	0.43	0.89	0.50	0.79
0.74	0.35	0.16	0.52	0.10	0.98	0.93	0.42

(a)	Construct a steam and leaf for the weight of the toys	[4 Marks]
(b)	Construct a frequency distribution for the weight of the toys	[6 Marks]
(c)	Use the frequency distribution you constructed in (b) to:	
	i. Construct an ogive and use it to estimate the quartiles	[8 Marks]
	ii. Calculate the coefficient of variation and interpret	[9 Marks]
	iii. On the ogive in (i), construct the box plot and interpret	[3 Marks]

- 2. An average light bulb manufactured by the Gudo Corporation lasts 300 days with a variance of 2 500 days.
  - a) What is the probability that a Gudo light bulb will last at most a year? [4 Marks]
  - b) The testing service reported to Gudo Corporation that one of its bulbs last at most X days with a probability of 0.96. Calculate the value of X? [4 Marks]
    c) State the two assumptions you made in (a) shows
  - c) State the two assumptions you made in (a) above [2 Marks]

### **SECTION B: ANSWER ANY THREE (3) QUESTIONS**

- **3.** A random variable is a variable whose value is determined by the outcome of a random experiment.
  - a) A company is trying to decide which one of two courses to institute. To help make a decision eight employees take Course 1 and another eight take Course 2. Each employee takes a test, which is graded out of a possible 25. The safety test results are shown below.

Course 1:	14	21	17	14	17	19	20	16
Course 2 :	20	18	22	15	23	21	19	15

i) Construct a 95% confidence interval for the difference of the means [7 Marks]

ii) Show that the sample mean is a consistent estimator of  $\mu$  [3 Marks]

- b) A farmer has 10 workers where 4 of them are female workers. A researcher randomly selects without replacement two workers for a survey. Based on the survey,
  - i) Construct a probability distribution with X as the random sample representing the number of male workers selected for the survey [6 Marks]
  - ii) Use the probability distribution you constructed in (i) to prove the probability conditions for discrete random variable [4 Marks]
- **4.** Statistical hypothesis testing is a decision making process for evaluating claims about a population.
  - a) At a local high school, students were randomly assigned to one of two Math teachers: Mrs Murairwa and Mrs Mukusha. After the assignment, Mrs Smith had 30 students, and Mrs Jones had 25 students. At the end of the year, each class took the same standardized test. Mrs Murairwa's students had an average test score of 78, with a standard deviation of 10; and Mrs Mukusha's students had an average test score of 85, with a standard deviation of 15. Use both traditional and p-value methods at 10% level of significance to test the hypothesis that the Math teachers are equally effective teachers [10 Marks]
  - b) A researcher claims that the average number of sports that colleges offer for males is greater than the average number of sports that colleges offer for females. A sample of the number of sports offered by colleges is shown in the table below:

		Males				Females						
6	11	11	8	15		6	8	11	13	8		
6	14	8	12	18		7	5	13	14	6		
6	9	5	6	9		6	5	5	7	6		
6	9	18	7	6	1	10	7	6	5	5		
15	6	11	5	5	1	16	10	7	8	5		
9	9	5	5	8		7	5	5	6	5		
8	9	6	11	6		9	18	13	7	10		
9	5	11	5	8		7	8	5	7	6		
7	7	5	10	7		11	4	6	8	7		
10	7	10	8	11	1	14	12	5	8	5		

At  $\alpha = 0.10$ , is there enough evidence to support the claim?

[10 Marks]

5. The cross tabulation of two survey questions produces the table shown below:

	Type of property									
How often	House	Fla	Bedsit	Other						
		t								
Once a	30	5	4	1						
month										
Once a week	110	80	8	2						
Twice a week	5	10	33	2						
More often	5	5	0	0						

(a) Construct an appropriate bar graph to show the distribution of the type of property [4

## Marks]

- (b) If one of the types of property is selected at random, find the probabilities that the: i) chosen property is not a house [2 Marks] ii) chosen property is Bedsit given that it has been used once a week [5 Marks]
- (c) State the three popular types of probability
- (d) At 5% level of significance, test whether there is an association between the two sets of responses for the two questions [6] Marks]
- 6. Probability is the chance of an event occurring.
  - (a) Assume that the tennis teams are evenly matched.
    - (i) What is the probability that the tennis match will last 4 games? [4 Marks]
    - (ii) Calculate the expected value and standard deviation of the probability distribution

[4 Marks]

[3 Marks]

- (b)An urn contains 6 red marbles and 4 black marbles. Two marbles are drawn from the urn without replacement.
  - i) What is the probability that both of the marbles are red?
  - [4 Marks] ii) What is the probability that a red marble and a black marble are drawn? [6 marks]
- (c) A business man has 4 shirts and 7 shorts. How many different shirt/short pair can the business man create? [2 Marks]

The end of paper

1. Sturge's Rule:  $C = 1 + 3.3 \log(n)$  $i > \frac{range}{C}$ Class width,  $=\frac{\sum_{i=1}^{n}fx_{i}}{x_{i}}$ 2. Mean of grouped data 3. Mean of ungrouped data =4. Mode =  $L_{mo} + \left(\frac{\Delta_1}{\Delta_1 + \Delta_2}\right) i$  $L_{me} + \left(\frac{\frac{n}{2} - F}{f_m}\right) i$  $5 \text{ Median} = \int_{me}^{\infty} \frac{1}{2\pi} \left(\frac{1}{2} - \frac{F}{f_m}\right) i$ viotic:  $= \sqrt{\frac{\sum_{i=1}^{n} fx_{i^2} - \frac{\left(\sum_{n=1}^{n} fx_i\right)^2}{n}}$ 6. Standard deviation  $\left| \sum_{i=1}^{n} x_{i^{2}}^{2} - \frac{1}{2} \right|$ 7. Standard Deviation of ungrouped data=  $S_k = \frac{3(mean - median)}{s} = \frac{mean - mod e}{s}$ 8. Coefficient of skewness:  $P(A\mathbf{i}) = \frac{P(A \cap B)}{P(A)}$ 9. Conditional probability: 10. Binomial Distribution:  $P(X=x)=nC_xp^xq^{n-x}$ 11. Poisson Distribution:  $P(X=x) = \frac{e^{-\lambda} \lambda^x}{x!}$ 12. Test statistic:  $t = \frac{\dot{X} - \mu}{\frac{s}{\sqrt{n}}}$  or  $Z = \frac{\dot{X} - \mu}{\frac{\sigma}{\sqrt{n}}}$ 13. Proportion Test Statistics =  $Z = \frac{\hat{p} - p}{\sqrt{pa/n}}$ 14.  $Z = \frac{X - \mu}{\sigma}$ 

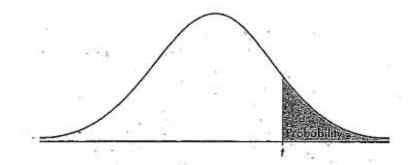
15. Weighted Mean: 
$$\dot{X}_{w} = \frac{\sum xw}{\sum w}$$
  
16.  $CV = \frac{s}{\dot{x}} \times 100$   
17.  $\hat{p} \cdot z_{\alpha/2} \sqrt{\frac{\hat{p}\hat{q}}{n}} 
18.  $E(X) = \sum X \cdot P(x)$   
19.  $\sigma = \sqrt{\sum x^{2}P(x) - \mu^{2}}$   
20.  $\overline{X} \cdot z_{\alpha/2} \left(\frac{\sigma}{\sqrt{n}}\right) < \mu < \overline{X} + z_{\alpha/2} \left(\frac{\sigma}{\sqrt{n}}\right)$   
21.  $z = \frac{(\overline{X}_{1} \cdot \overline{X}_{2}) \cdot (\mu_{1} - \mu_{2})}{\sqrt{\frac{\sigma_{1}^{2}}{n_{1}} + \frac{\sigma_{2}^{2}}{n_{2}}}}$  or  $t = \frac{(\overline{X}_{1} - \overline{X}_{2}) \cdot (\mu_{1} - \mu_{2})}{\sqrt{\frac{s_{1}^{2}}{n_{1}} + \frac{s_{2}^{2}}{n_{2}}}}$   
22.  $(\overline{X}_{1} - \overline{X}_{2}) - z_{\alpha/2} \sqrt{\frac{\sigma_{1}^{2}}{n_{1}} + \frac{\sigma_{2}^{2}}{n_{2}}} < (\mu_{1} - \mu_{2}) < (\overline{X}_{1} - \overline{X}_{2}) + z_{\alpha/2} \sqrt{\frac{\sigma_{1}^{2}}{n_{1}} + \frac{\sigma_{2}^{2}}{n_{2}}}}$$ 

$$23. t = \frac{\overline{D} - \mu_D}{s_D / \sqrt{n}}$$

24. 
$$z = \frac{(\hat{p}_{1} - \hat{p}_{2}) - (p_{1} - p_{2})}{\sqrt{pq} \left(\frac{1}{n_{1}} + \frac{1}{n_{2}}\right)}$$
where

 $\overline{p} = \frac{X_1 + X_2}{n_1 + n_2} \quad \hat{p}_1 = \frac{X_1}{n_1}$  $\overline{q} = 1 - \overline{p} \qquad \hat{p}_2 = \frac{X_2}{n_2}$ 

25. 
$$\chi^2 = \sum \frac{(O-E)^2}{E}$$



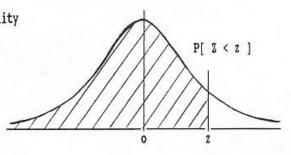
#### TABLE B: #-DISTRIBUTION CRITICAL VALUES

$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$					4	Tai	l probabi	lity p				•	
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	ďď	.25	.20	.15	.10	.05	.025	.02	.01	.005	.0025	.001	.000
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	1	1.000	1.376	1.963	3.078	6.314	12.71	15.89	31.82	63.66	127.3	318.3	636.
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	2	.816	1.061	1.386	1.886	2.920	4.303	4.849	6.965	9.925	14.09		31.6
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		.765	.978	1.250	1.638	2.353	3,182	3.482	4.541	5.841			12.9
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	4	.741	.941	1.190	1.533	2.132	2.776	2.999	3.747	4.604	5.598	7.173	8.61
	5	.727	.920	1.156	1.476	2.015	2.571	2.757	3.365	4.032			6.86
		.718	.906	1.134	1.440	1.943	2.447	2.612	3.143	3.707	4.317	5.208	5.95
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	7	.711		1.119	1.415	1.895	2.365	2.517	2.998	3.499	4.029	4.785	5.40
	8	.706	.889	1.108	1.397	1.860	2.306	2.449	2.896	3.355	3.833	4.501	5:04
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	9		.883	1.100	1.383	1.833	2.262	2.398	2.821	3.250	3.690	4.297	4.78
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$										3.169		4.144	4.58
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	11						2,201	2.328	2:718	3.106	3.497	4.025	4.43
$\begin{array}{cccccccccccccccccccccccccccccccccccc$										3.055	3.428	3.930	4.31
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	13							2.282	2.650	3.012	3.372	3.852	4.22
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$									2.624	2.977	3.326	3.787	4.14
$\begin{array}{cccccccccccccccccccccccccccccccccccc$										2.947	3.286	3.733	4.073
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	16		.865	1.071		1.746	2.120	2.235	2.583	2.921	3.252-	3.686	4.01:
$\begin{array}{cccccccccccccccccccccccccccccccccccc$							2.110	2.224	2.567	2.898	3.222	3.646	3.96
$\begin{array}{cccccccccccccccccccccccccccccccccccc$										2.878	3.197	3.611	3.92
$\begin{array}{cccccccccccccccccccccccccccccccccccc$							2.093		2.539	2.861	3.174	3.579	3.883
$\begin{array}{cccccccccccccccccccccccccccccccccccc$						1.725	2.086	2.197	2.528	2.845	3.153	3.552	3.850
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		.686	.859	1.063	1.323	1.721	2.080	2.189	2.518	2.831	3.135	3.527	3.819
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$				1.061		1.717	2.074	2.183	2.508	2.819	3.119	3.505	3.792
$\begin{array}{cccccccccccccccccccccccccccccccccccc$				1.060	1.319	1.714	2.069	2.177	2.500	2.807	3.104	3.485	3.768
$\begin{array}{cccccccccccccccccccccccccccccccccccc$			.857	1.059	1.318	1.711	2.064	2.172	2.492	2.797	3.091	3.467.	3.74
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	25	.684	.856	1.058	1.316	1.708	2.060	2.167	2.485	2.787	3.078	3.450	3.72
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$			.856	1.058	1.315	1.706	2.056	2.162	2.479	2.779	3.067	3.435	3.70
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	27	.684	.855	1.057	1.314	1.703	2.052	2.158	2.473	2.771	3.057	3.421	3.690
$\begin{array}{cccccccccccccccccccccccccccccccccccc$							2.048	2.154	2.467	2.763	3.047	3.408	3.674
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	29	.683	.854	1.055	1.311	1.699	2.045	2.150	2.462	2.756	3.038	3.396	3.659
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	30		.854	1.055	1.310	1.697	2.042	2.147	2:457	2.750	3.030	3.385	3.646
							2.021		2.423	2.704		3.307	3.551
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	50		.849	1.047	1.299	1.676	2.009	2.109	2.403	2.678	2.937	3.261	3.496
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$			.848	1.045			2.000	2.099	2.390	2.660	2.915	3.232	3.460
$\begin{array}{cccccccccccccccccccccccccccccccccccc$							1.990	2.088	2.374	2.639	2.887		3.416
$            \begin{array}{ccccccccccccccccccccccccc$		.677	.845		1.290	1.660	1.984	2.081	2.364				3.390
∞ .674 .841 1.036 1.282 1.645 1.960 2.054 2.326 2.576 2.807 3.091 3.29	1000						1.962	2.056	2.330				3.300
50% 60% 70% 80% 90% 95% 96% 98% 99% 99.5% 99.8% 99.9	00	.674	.841	1.036	1.282	1.645	1.960	2.054	2.326				3.291
		50%	60%	70%	80%	90%	95%	96%	98%	99%	99.5%	99.8%	99.99

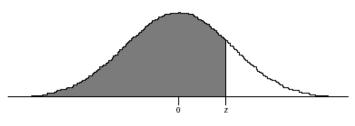
## 1. Areas under the Normal Distribution

The table gives the cumulative probability up to the standardised normal value z i.e. z

 $P[Z < z] = \int_{-\infty}^{\infty} \frac{1}{\sqrt{2\pi}} \exp(-\frac{1}{2}Z^2) dZ$ 



Z	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.0	0.5000	0.5040	0.5080	0.5120	0.5159	0.5199	0.5239	0.5279	0.5319	0.5359
0.1	0.5398	0.5438	0.5478	0.5517	0.5557	0.5596	0.5636	0.5675	0.5714	0.5753
0.2	0.5793	0.5832	0.5871	0.5910	0.5948	0.5987	0.6026	0.6064	0.6103	0.6141
0.3	0.6179	0.6217	0.6255	0.6293	0.6331	0.6368	0.6406	0.6443	0.6480	0.6517
0.4	0.6554	0.6591	0.6628	0.6664	0.6700	0.6736	0.6772	0.6808	0.6844	0.6879
0.5	0.6915	0.6950	0.6985	0.7019	0.7054	0.7088	0.7123	0.7157	0.7190	0.7224
0.6	0.7257	0.7291	0.7324	0.7357	0.7389	0.7422	0.7454	0.7486	0.7517	0.7549
0.7	0.7580	0.7611	0.7642	0.7673	0.7704	0.7734	0.7764	0.7794	0.7823	0.7854
0.8	0.7881	0.7910	0.7939	0.7967	0.7995	0.8023	0.8051	0.8078	0.8106	0.8133
0.9	0.8159	0.8186	0.8212	0.8238	0.8264	0.8289	0.8315	0.8340	0.8365	0.8389
1.0	0.8413	0.8438	0.8461	0.8485	0.8508	0.8531	0.8554	0.8577	0.8599	0.8621
1.1	0.8643	0.8665	0.8686	0.8708	0.8729	0.8749	0.8770	0.8790	0.8804	0.8830
1.2	0.8849	0.8869	0.8888	0.8907	0.8925	0.8944	0.8962	0.8980	0.8997	0.9015
1.3	0.9032	0.9049	0.9066	0.9082	0.9099	0.9115	0.9131	0.9147	0.9162	0.9177
1.4	0.9192	0.9207	0.9222	0.9236	0.9251	0.9265	0.9279	0.9292	0.9306	0.9319
1.5	0.9332	0.9345	0.9357	0.9370	0.9382	0.9394	0.9406	0.9418	0.9429	0.9441
1.6	0.9452	0.9463	0.9474	0.9484	0.9495	0.9505	0.9515	0.9525	0.9535	0.9545
1.7	0.9554	0.9564	0.9573	0.9582	0.9591	0.9599	0.9608	0.9616	0.9625	0.9633
1.8	0.9641	0.9649	0.9656	0.9664	0.9671	0.9678	0.9686	0.9693	0.9699	0.9706
1.9	0.9713	0.9719	0.9726	0.9732	0.9738	0.9744	0.9750	0.9756	0.9761	0.9767
2.0	0.9773	0.9778	0.9783	0.9788	0.9793	0.9798	0.9803	0.9808	0.9812	0.9817
2.1	0.9821	0.9826	0.9830	0.9834	0.9838	0.9842	0.9846	0.9850	0.9854	0.9857
2.2	0.9861	0.9865	0.9868	0.9871	0.9874	0.9878	0.9881	0.9884	0.9887	0.9890
2.3	0.9893	0.9896	0.9898	0.9901	0.9904	0.9906	0.9909	0.9911	0.9913	0.9916
2.4	0.9918	0.9920	0.9922	0.9924	0.9927	0.9929	0.9931	0.9932	0.9934	0.9936
2.5	0.9938	0.9940	0.9941	0.9943	0.9945	0.9946	0.9948	0.9949	0.9951	0.9952
2.6	0.9953	0.9955	0.9956	0.9957	0.9959	0.9960	0.9961	0.9962	0.9963	0.9964
2.7	0.9965	0.9966	0.9967	0.9968	0.9969	0.9970	0.9971	0.9972	0.9973	0.9974
2.8	0.9974	0.9975	0.9976	0.9977	0.9977	0.9978	0.9979	0.9980	0.9980	0.9981
2.9	0.9981	0.9982	0.9982	0.9983	0.9984	0.9984	0.9985	0.9985	0.9986	0.9986
z	3.00	3.10	3.20	3.30	3.40	3.50	3.60	3.70	3.80	3.90
P	0.9986	0.9990	0.9993	0.9995	0.9997	0.9998	0.9998	0.9999	0.9999	1.0000



Norma Deviat										
z	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
- 4.0	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000
-3.9	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000
-3.8	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000
-3.7	.0001	.0001	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000
-3.6	.0002	.0002	.0001	.0001	.0001	.0001	.0001	.0001	.0001	.0001
-3.5	.0002	.0002	.0002	.0002	.0002	.0002	.0002	.0002	.0002	.0002
-3.4	.0003	.0003	.0003	.0003	.0003	.0003	.0003	.0003	.0003	.0002
-3.3	.0005	.0005	.0005	.0004	.0004	.0004	.0004	.0004	.0004	.0003
-3.2	.0007	.0007	.0006	.0006	.0006	.0006	.0006	.0005	.0005	.0005
-3.1	.0010	.0009	.0009	.0009	.0008	.0008	.0008	.0008	.0007	.0007
-3.0	.0013	.0013	.0013	.0012	.0012	.0011	.0011	.0011	.0010	.0010
-2.9	.0019	.0018	.0018	.0017	.0016	.0016	.0015	.0015	.0014	.0014
-2.8	.0026	.0025	.0024	.0023	.0023	.0022	.0021	.0021	.0020	.0019
-2.7	.0035	.0034	.0033	.0032	.0031	.0030	.0029	.0028	.0027	.0026
-2.6	.0047	.0045	.0044	.0043	.0041	.0040	.0039	.0038	.0037	.0036
-2.5	.0062	.0060	.0059	.0057	.0055	.0054	.0052	.0051	.0049	.0048
-2.4	.0082	.0080	.0078	.0075	.0073	.0071	.0069	.0068	.0066	.0064
-2.3	.0107	.0104	.0102	.0099	.0096	.0094	.0091	.0089	.0087	.0084
-2.2	.0139	.0136	.0132	.0129	.0125	.0122	.0119	.0116	.0113	.0110
-2.1	.0179	.0174	.0170	.0166	.0162	.0158	.0154	.0150	.0146	.0143
-2.0	.0228	.0222	.0217	.0212	.0207	.0202	.0197	.0192	.0188	.0183
-1.9	.0287	.0281	.0274	.0268	.0262	.0256	.0250	.0244	.0239	.0233
-1.8	.0359	.0351	.0344	.0336	.0329	.0322	.0314	.0307	.0301	.0294
-1.7	.0446	.0436	.0427	.0418	.0409	.0401	.0392	.0384	.0375	.0367
-1.6	.0548	.0537	.0526	.0516	.0505	.0495	.0485	.0475	.0465	.0455
-1.5	.0668	.0655	.0643	.0630	.0618	.0606	.0594	.0582	.0571	.0559
-1.4	.0808	.0793	.0778	.0764	.0749	.0735	.0721	.0708	.0694	.0681
-1.3	.0968	.0951	.0934	.0918	.0901	.0885	.0869	.0853	.0838	.0823
-1.2	.1151	.1131	.1112	.1093	.1075	.1056	.1038	.1020	.1003	.0985
-1.1	.1357	.1335	.1314	.1292	.1271	.1251	.1230	.1210	.1190	.1170
-1.0	.1587	.1562	.1539	.1515	.1492	.1469	.1446	.1423	.1401	.1379
0	.1841	.1814	.1788	.1762	.1736	.1711	.1685	.1660	1625	.1611
9 8	.1841	.1814	.2061	.2033	.2005	.1977	.1949	.1922	.1635 .1894	.1867
0	.2420	.2389	.2358	.2033	.22005	.2266	.2236	.2206	.2177	.2148
6	.2743	.2709	.2676	.2643	.2611	.2578	.2546	.2514	.2483	.2451
5	.3085	.3050	.3015	.2981	.2946	.2912	.2877	.2843	.2810	.2776
4	2446	.3409	2270	.3336	.3300	.3264	.3228	2102	2156	.3121
4 3	.3446 .3821	.3409 .3783	.3372 .3745	.3336	.3300	.3264 .3632	.3228 .3594	.3192 .3557	.3156 .3520	.3121
3	.3021	.3163	.5745	.3101	.3009	.3032	.5594	.5007	.5520	.0400

Chi Squared Distribution Table

$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	5.635     7       9.21     1       11.345     1       13.277     1       15.086     1	0.005 7.879 10.597 12.838 14.86
20.010.020.0510.1030.2114.6055.9917.378930.0720.1150.2160.3520.5846.2517.8159.348140.2070.2970.4840.7111.0647.7799.48811.143150.4120.5540.8311.1451.619.23611.0712.8331	9.21     1       11.345     1       13.277     1       15.086     1	10.597 12.838 14.86
3         0.072         0.115         0.216         0.352         0.584         6.251         7.815         9.348         1           4         0.207         0.297         0.484         0.711         1.064         7.779         9.488         11.143         1           5         0.412         0.554         0.831         1.145         1.61         9.236         11.07         12.833         1	11.345113.277115.0861	12.838 14.86
40.2070.2970.4840.7111.0647.7799.48811.143150.4120.5540.8311.1451.619.23611.0712.8331	13.277 1 15.086 1	14.86
5 0.412 0.554 0.831 1.145 1.61 9.236 11.07 12.833 1	15.086 1	
5 0.412 0.554 0.831 1.145 1.61 9.236 11.07 12.833 1		16 75
6 0 676 0 872 1 227 1 625 2 204 10 645 12 502 14 440 1	16.812 1	16.75
0   0.070   0.872   1.237   1.033   2.204   10.043   12.392   14.449   1	10.012	18.548
	18.475 2	20.278
8 1.344 1.646 2.18 2.733 3.49 13.362 15.507 17.535 2	20.09 2	21.955
9 1.735 2.088 2.7 3.325 4.168 14.684 16.919 19.023 2	21.666 2	23.589
10 2.156 2.558 3.247 3.94 4.865 15.989 18.307 20.483 2	23.209 2	25.188
11 2.603 3.053 3.816 4.575 5.578 17.275 19.675 21.92 2	24.725 2	26.757
12 3.074 3.571 4.404 5.226 6.304 18.549 21.026 23.337 2	26.217 2	28.3
13 3.565 4.107 5.009 5.892 7.042 19.812 22.362 24.736 2	27.688 2	29.819
14 4.075 4.66 5.629 6.571 7.79 21.064 23.685 26.119 2	29.141 3	31.319
15 4.601 5.229 6.262 7.261 8.547 22.307 24.996 27.488 3	30.578 3	32.801
16 5.142 5.812 6.908 7.962 9.312 23.542 26.296 28.845 3	32 3	34.267
17 5.697 6.408 7.564 8.672 10.085 24.769 27.587 30.191 3	33.409 3	35.718
	34.805 3	37.156
		38.582
20 7.434 8.26 9.591 10.851 12.443 28.412 31.41 34.17 3	37.566 3	39.997
21 8.034 8.897 10.283 11.591 13.24 29.615 32.671 35.479 3	38.932 4	41.401
22 8.643 9.542 10.982 12.338 14.041 30.813 33.924 36.781 4	40.289 4	42.796
23 9.26 10.196 11.689 13.091 14.848 32.007 35.172 38.076 4	41.638 4	44.181
	42.98 4	45.559
25 10.52 11.524 13.12 14.611 16.473 34.382 37.652 40.646 4	44.314 4	46.928
26 11.16 12.198 13.844 15.379 17.292 35.563 38.885 41.923 4	45.642 4	48.29
27 11.808 12.879 14.573 16.151 18.114 36.741 40.113 43.195 4	46.963 4	49.645
28 12.461 13.565 15.308 16.928 18.939 37.916 41.337 44.461 4	48.278 5	50.993
29 13.121 14.256 16.047 17.708 19.768 39.087 42.557 45.722 4	49.588 5	52.336
	50.892 5	53.672
	63.691 6	66.766
	76.154	79.49
	88.379 9	91.952
	100.425 1	104.215
80 51.192 53.54 57.153 60.391 64.278 96.578 101.879 106.629 1	112.329 1	116.321
90 59.196 61.754 65.647 69.126 73.291 107.565 113.145 118.136 1	124.116	128.294
	135.807 1	140.169